

An OpenCL ray tracing approach for Simulating Electromagnetic Fields



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PHPC2012 - 13 december 2012

- **Context description**
- **An adapted sequential ray tracing algorithm**
- **First attempt to accelerate by implementing parallel computing**

Real life situations



Verification by measurement



- High electric field strengths E [V/m]
- Unpredictable environment
- Risk of failure or loss of performance
- Predictable, controlled and repetitive
- According to standard:
 - MIL-STD-461E RS103
 - RTCA DO160E
 - EN61000-4-21
- SAR, FAR, OATS, Reverberation chamber

RVC Loading and field uniformity verification

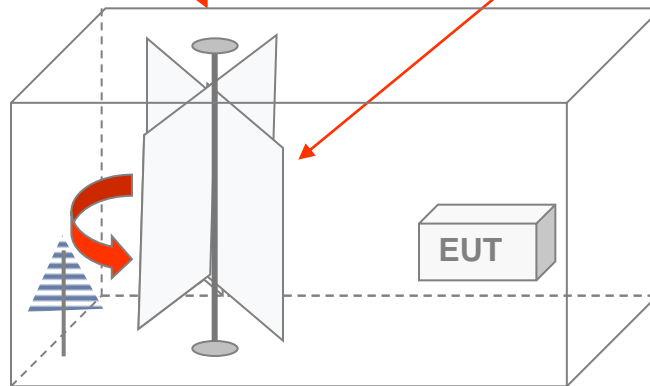
- Goal: High field strength with moderate input power,

statistically homogeneous and with random polarization

*High reflection rate
=> High Q factor,
=> standing waves*

*Continuously changing
boundary conditions*

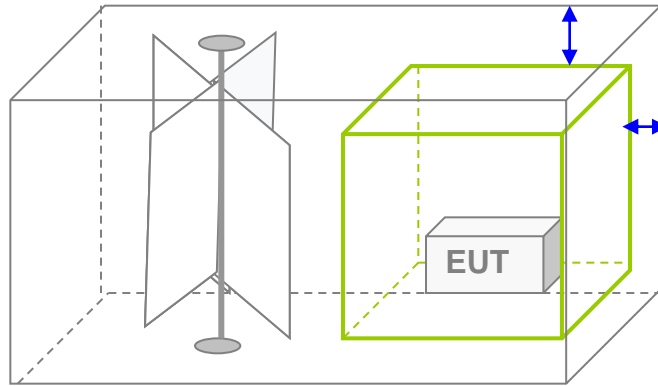
- RVC Characteristics:
Overmoded highly conductive cavity with mode stirrer



RVC Loading and field uniformity verification

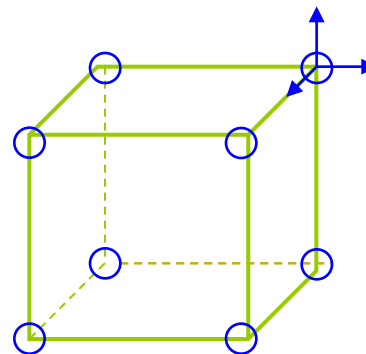
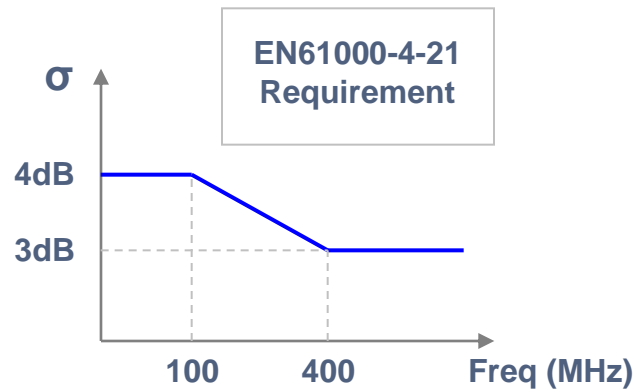
- Virtual test volume:

minimum distance between wall and EUT $\sim \lambda_{LF}$ (EN61000-4-21: $1/3 \cdot \lambda_{LF}$)



- Empty chamber field uniformity:

8 corner points,
3 field values $|E_x|$, $|E_y|$ and $|E_z|$ (max over 2π stirrer rotation)
 \Rightarrow 24 values in total



- Influence of EUT on field uniformity:

- EUT absorption/reflection => chamber loading may exceed maximum
- Field uniformity requirements (low statistical field deviation) exceeded ?

- Preliminary chamber loading verification needed (with EUT in place) (CLF: EN61000-4-21, Annex B, par.B.2)

- Additional test time (equipment, test engineer, EUT availability?)

- Additional \$\$!!

To be avoided ...

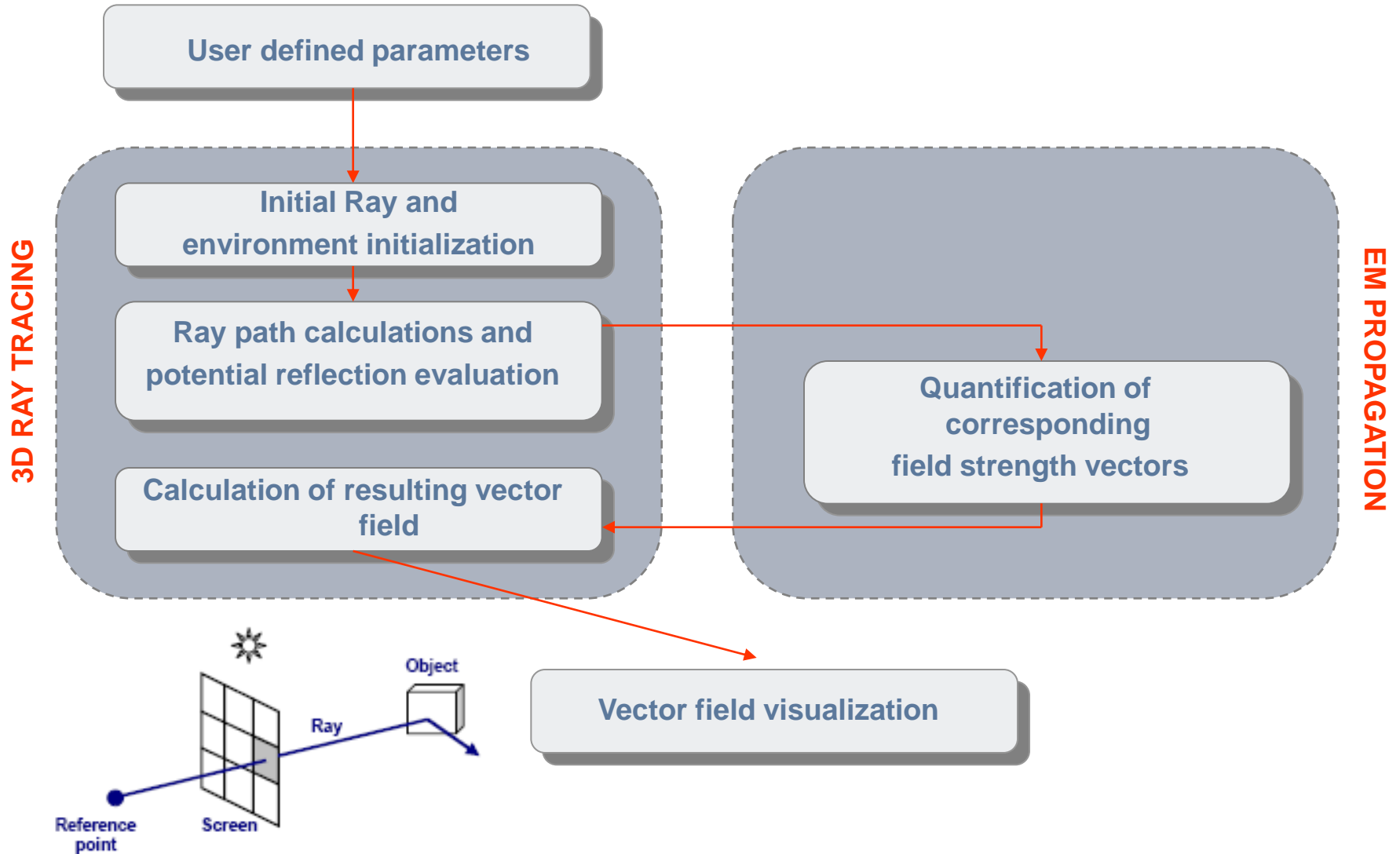
Determination of $|E_x|$, $|E_y|$ and $|E_z|$ required

- at 8 cornerpoints
- for each frequency
- for arbitrary mode stirrer angles
- for given input power
- for a given Tx antenna



Modeling of 3D field propagation

Adapted Ray Tracing



Adapted Ray Tracing

a) Basic Ray Tracing

• Ray equation

$$p = p_0 + s \cdot \vec{u}$$

• Plane equation

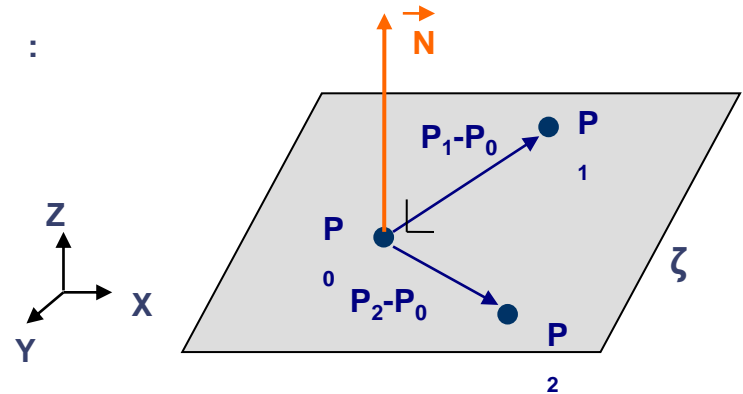
Given non-collinear points p_0, p_1, p_2 on plane ζ in 3D Cartesian coordinate system,
plane equation can be derived $\forall p(x,y,z) \in \zeta$:

$$\vec{N} \bullet \vec{P} = -D$$

with \vec{N} : surface normal

\vec{P} : point on plane ζ

D : plane specific C^{te}

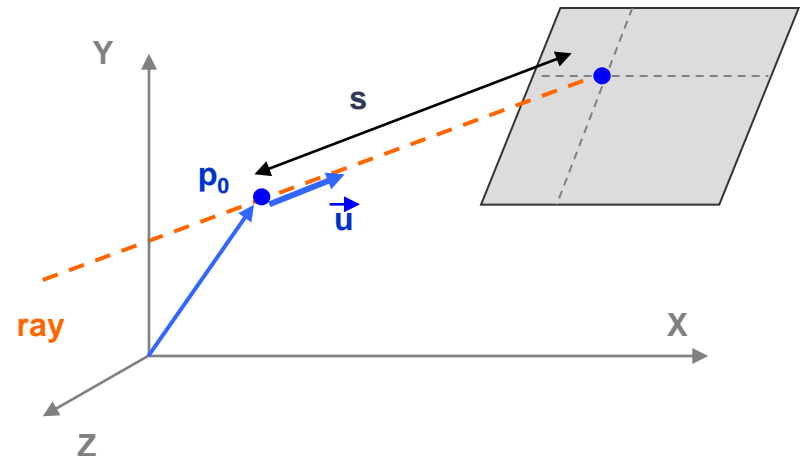


• Ray – surface intersection

$$\begin{cases} P = P_0 + s\vec{u} \\ \vec{N} \bullet P = -D \end{cases}$$

$$\equiv \vec{N} \bullet (P_0 + s\vec{u}) = -D$$

$$\equiv s = \frac{-D - \vec{N} \bullet P_0}{\vec{N} \bullet \vec{u}}$$

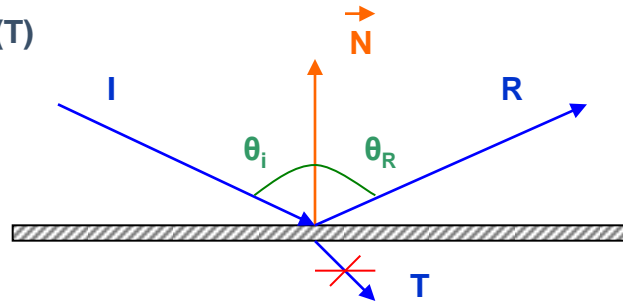


- Ray reflection

Reflection of EM waves on panel surface

Specular reflection is assumed (no diffuse spreading): law of regular reflection: $\theta_i = \theta_r$

No refraction (T)

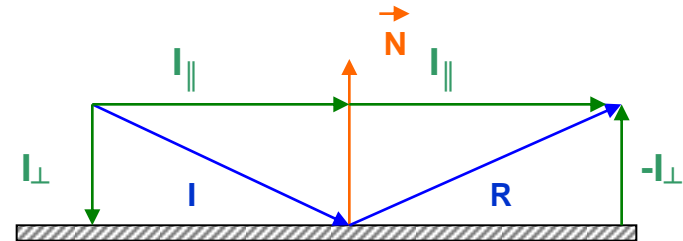


Calculation of reflected ray equation R needed:

$$\vec{R} = \overbrace{(\vec{I} - (\vec{I} \cdot \vec{N}) \cdot \vec{N})}^{I_{\parallel}} - \overbrace{(\vec{I} \cdot \vec{N}) \cdot \vec{N}}^{I_{\perp}}$$

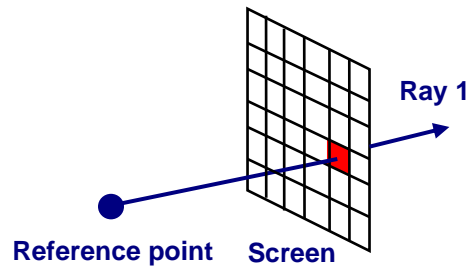
$$\equiv$$

$$\vec{R} = \vec{I} - (2 \cdot \vec{I} \cdot \vec{N}) \cdot \vec{N}$$



b) Adaptation of standard Ray Tracing

- Multiple viewpoints instead of one



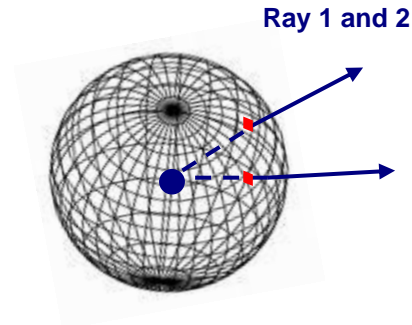
Basic ray tracing

1 viewpoint
=> 1 ray / pixel

Ray origin: viewpoint

No attenuation

No phase information



Adapted ray tracing

multiple omnidirectional (or isotropic) viewpoints
(inside virtual volume)

Ray origin: Transmit antenna
(alternative backtracking algorithm)

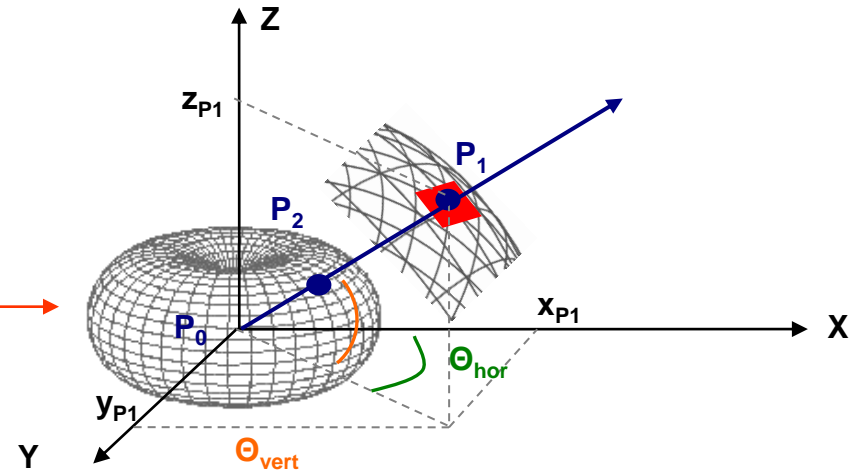
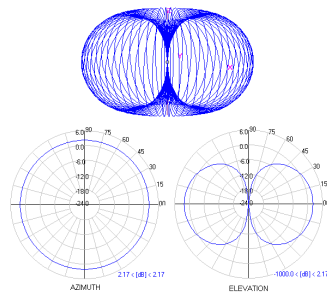
attenuation and phase calculation



Adapted Ray Tracing

- Adjustment 1: ray origin = source antenna

Allows 3D interpolation of radiation pattern (dBi)



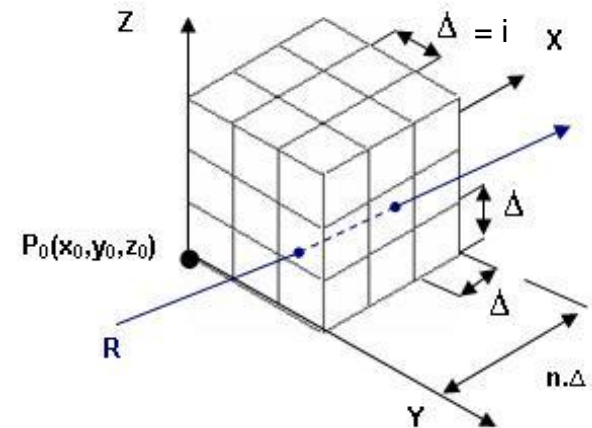
- Adjustment 2: Spatial subdivision needed

due to initial angle step at ray origin

=> Association of each viewpoint with cubic volume

avoids missing viewpoints

when minimum angle $\alpha = 2 \cdot \arcsin\left(\frac{i/2}{n \cdot L}\right)$



REMARK: avoid taking **same wavefront** into account more then once

Adapted Ray Tracing

- Adjustment 3: Quantification of EM field strength vectors

- Amplitude and phase: related to total ray traveling distance (r)

- For far field, free space, tuned dipole:

$$|\vec{E}_\theta| = j \cdot \frac{Z_0 \cdot I_m}{2\pi r} \cdot e^{-j \cdot k \cdot r} \left[\frac{\cos(k \cdot L/2 \cdot \cos \theta) - \cos(k \cdot L/2)}{\sin \theta} \right]$$

$$\frac{Z_0 \cdot I_m}{2\pi r}$$

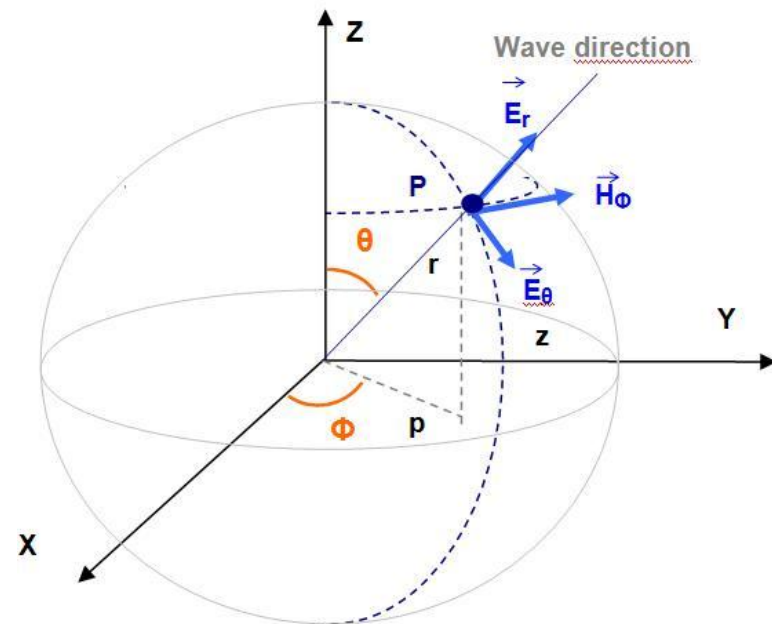
amplitude (~ 1 / r)

$$j \cdot e^{-j \cdot k \cdot r}$$

phase (~ r)

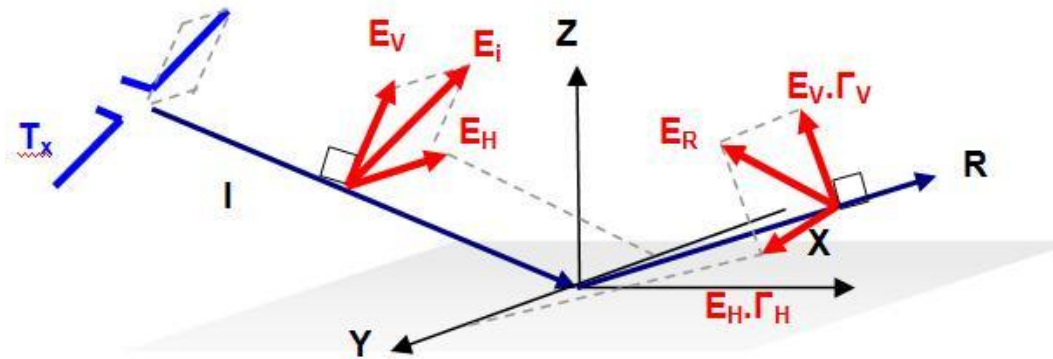
$$\left[\frac{\cos(k \cdot L/2 \cdot \cos \theta) - \cos(k \cdot L/2)}{\sin \theta} \right]$$

tuned dipole radiation pattern (F(θ))



Adapted Ray Tracing

- Adjustment 4: EM wave reflection



$$\Gamma_H = \frac{\cos \theta - \sqrt{N_d^2 - \sin^2 \theta}}{\cos \theta + \sqrt{N_d^2 - \sin^2 \theta}}$$

$$\Gamma_V = \frac{N_d^2 \cos \theta - \sqrt{N_d^2 - \sin^2 \theta}}{N_d^2 \cos \theta + \sqrt{N_d^2 - \sin^2 \theta}}$$

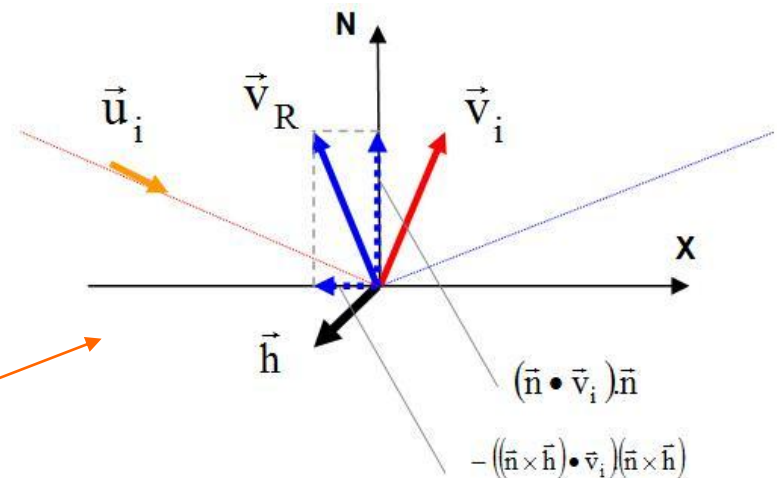
- reflection coefficients approximation: $\Gamma_H = -1$ and $\Gamma_V = 1$ for ideal conducting material
- Vector reorientation after reflection:

$$\vec{E}_R = |\vec{E}_H| \Gamma_H \vec{h} + |\vec{E}_V| \Gamma_V \vec{v}_R$$

$$|\vec{E}_H| = \vec{E}_i \cdot \vec{h}$$

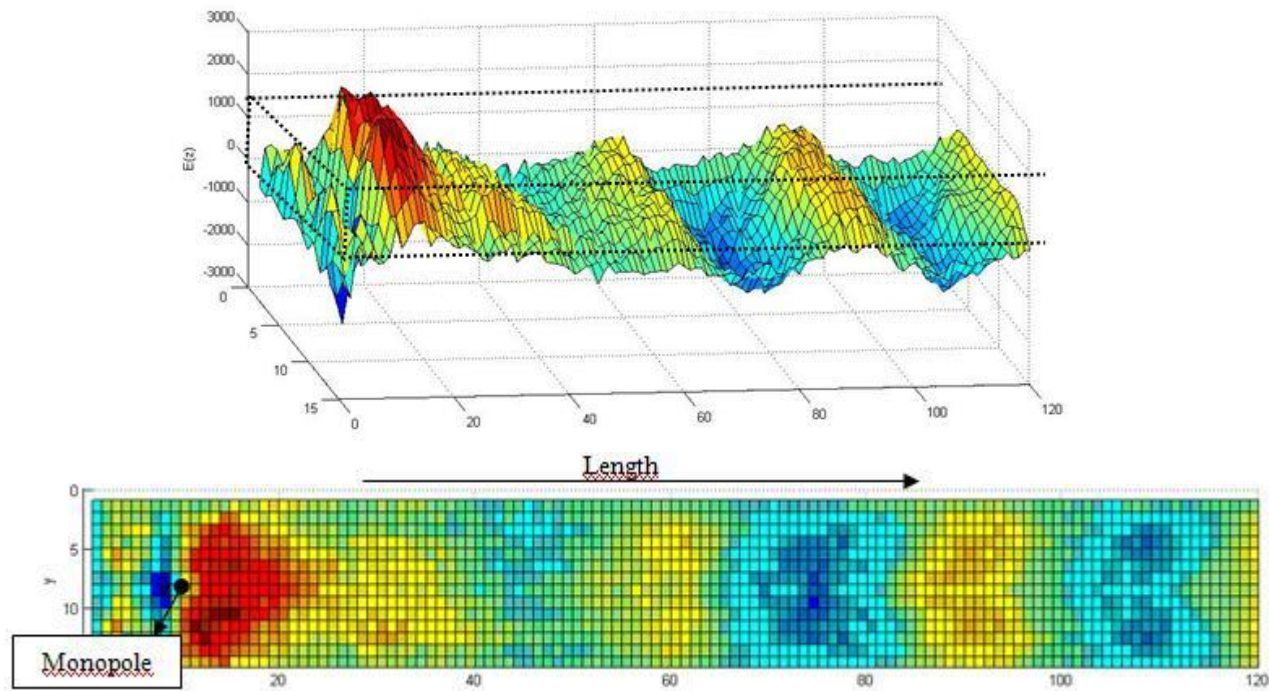
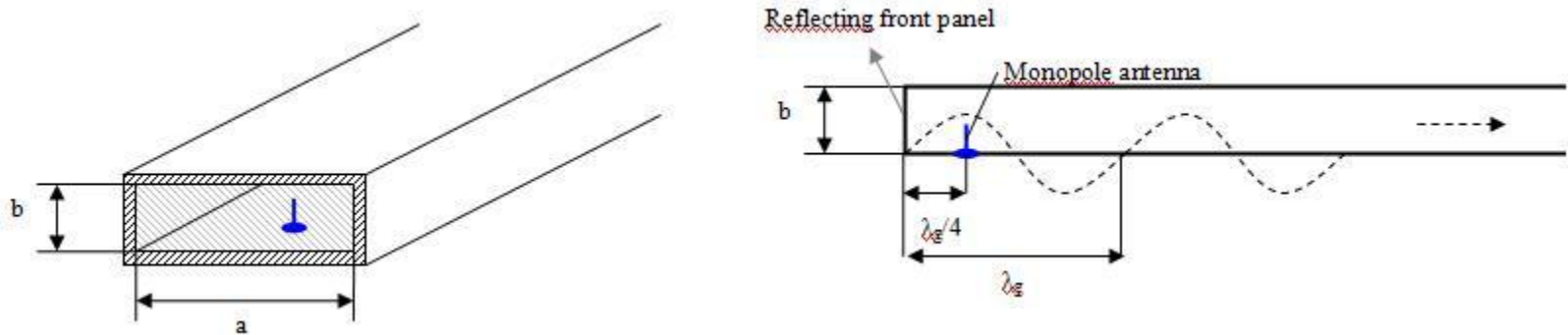
$$\vec{E}_V = \vec{E}_i - \vec{E}_H$$

$$\vec{v}_R = (\vec{n} \cdot \vec{v}_i) \vec{n} - ((\vec{n} \times \vec{h}) \cdot \vec{v}_i) (\vec{n} \times \vec{h})$$



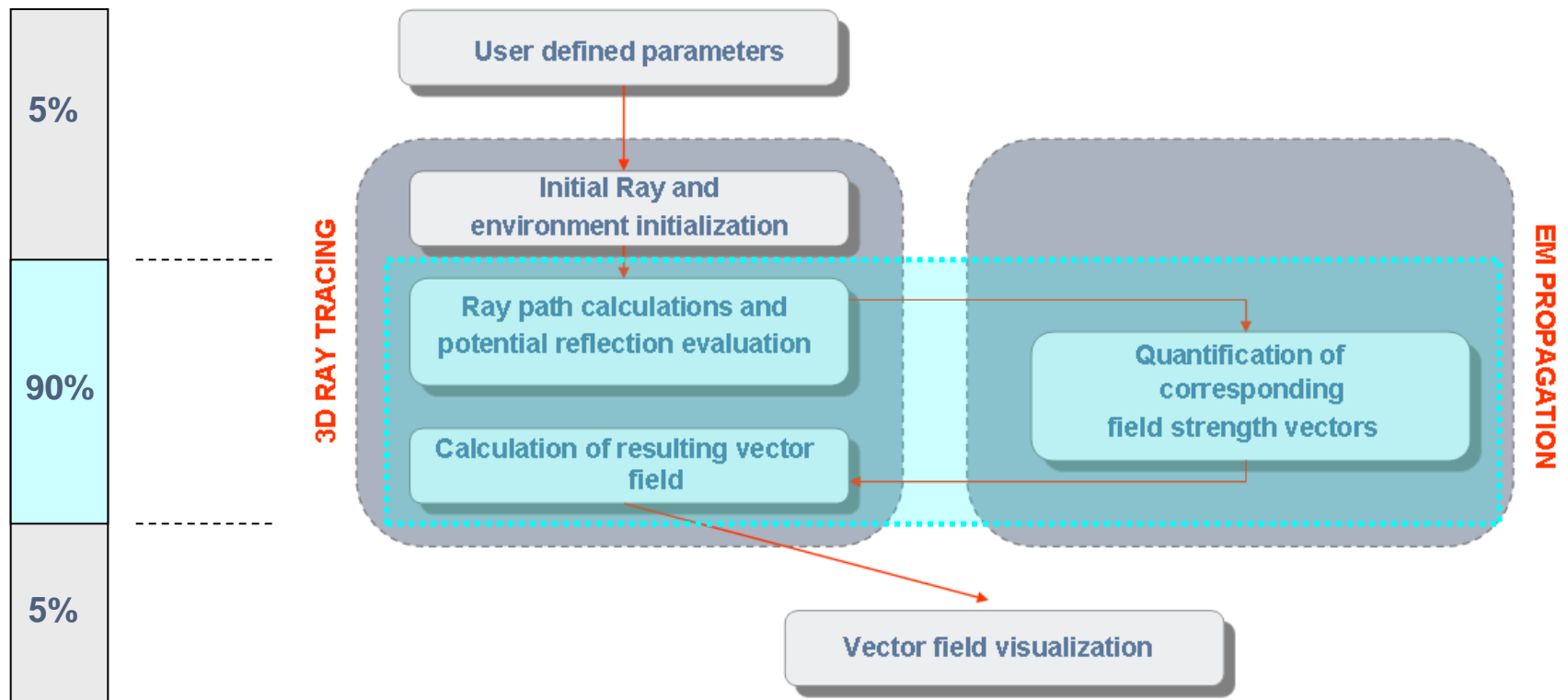
Example after visualization

- TE_{10} waveguide



OpenCL implementation

- Can parallel computing be a useful acceleration technique?
⇒ which code can be run in parallel?



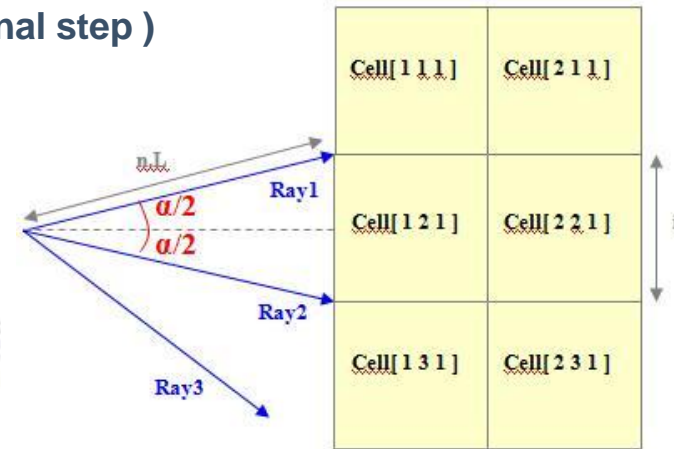
Amdahl's Law:

$$\begin{aligned}\text{maximum speedup } S &= (T_s + T_p) / (T_s + T_p/N) \\ &= 1 / y \quad \text{with } y = 10\% \\ &= \mathbf{10}\end{aligned}$$

- **Data parallelism** more suitable than Task parallelism
 - Each ray has **individual** contribution to 3D vector field
 - no **data dependency** in between ray calculations
(Resulting vector field is determined as separate final step)
- **Memory consumption** related to **accuracy**

$$\alpha = 2 \cdot \arcsin\left(\frac{i/2}{nL}\right) \quad \text{where } i = \text{cell size},$$

$n = \text{max number of reflections},$
 $L = \text{longest chamber dimension (3D diagonal between two opposite corners).}$



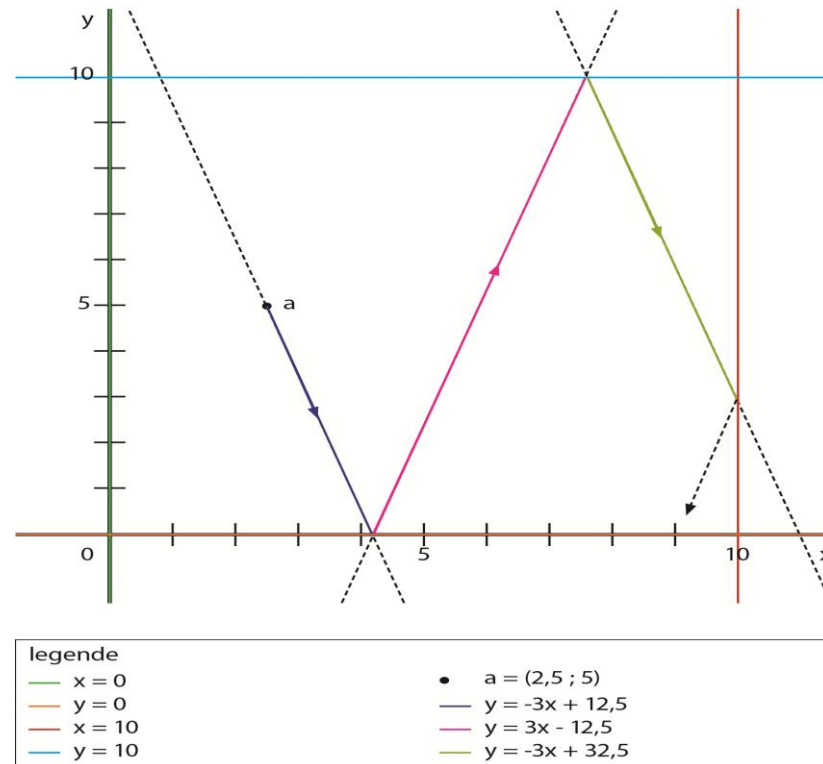
“Poor” approach:

- a)
- $1 \text{ GHz} \Rightarrow i = \lambda / (2 \cdot 10) = 0,003\text{m} \text{ (10 samples per wavelength)}$
 $\text{cavity } 5\text{m} \times 5\text{m} \times 10\text{m} \Rightarrow L = 11,45 \text{ m}$
 $n = 10$
- $\alpha = 75^{\circ} \Rightarrow \quad \# \text{ initial rays: } 173^{E06}$
 $\text{for each ray: 3 floats} \Rightarrow 12 \text{ bytes} \times 173^{E06}$
 $= \text{ca. } 2,07 \text{ GB}$
- b) for each viewpoint: 2 floats \Rightarrow e.g. $9\text{m}^3 = 8 \text{ bytes} \times 10^6 = \text{ca. } 295 \text{ MB}$

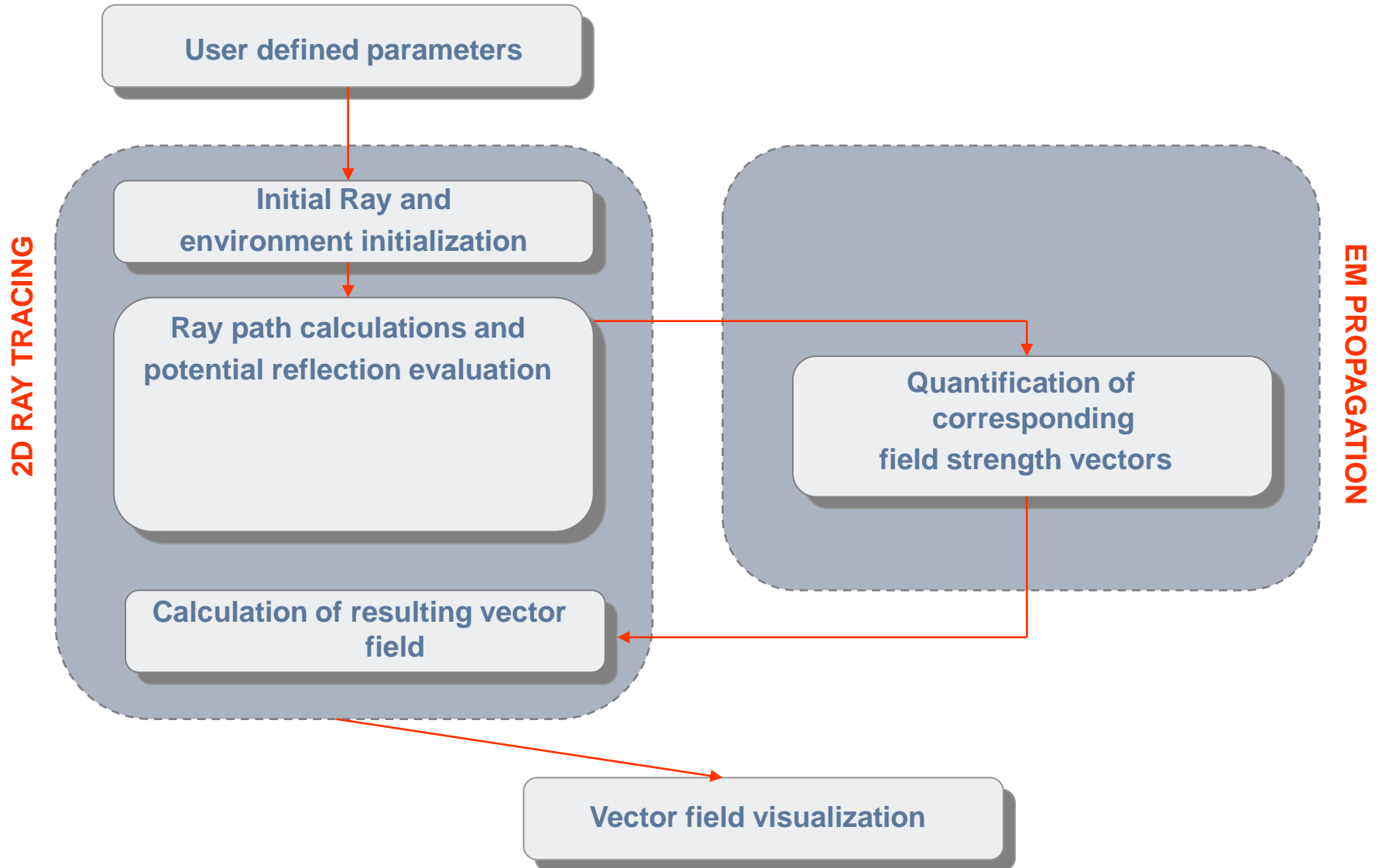
- Parallel calculation of a **limited** set of ray tracers
 - Number of rays per set depending on # processing units
 - Calculate contribution of full ray path of each set, then continue with next set
=> avoids memory overflow for intermediate results

- 2D Implementation

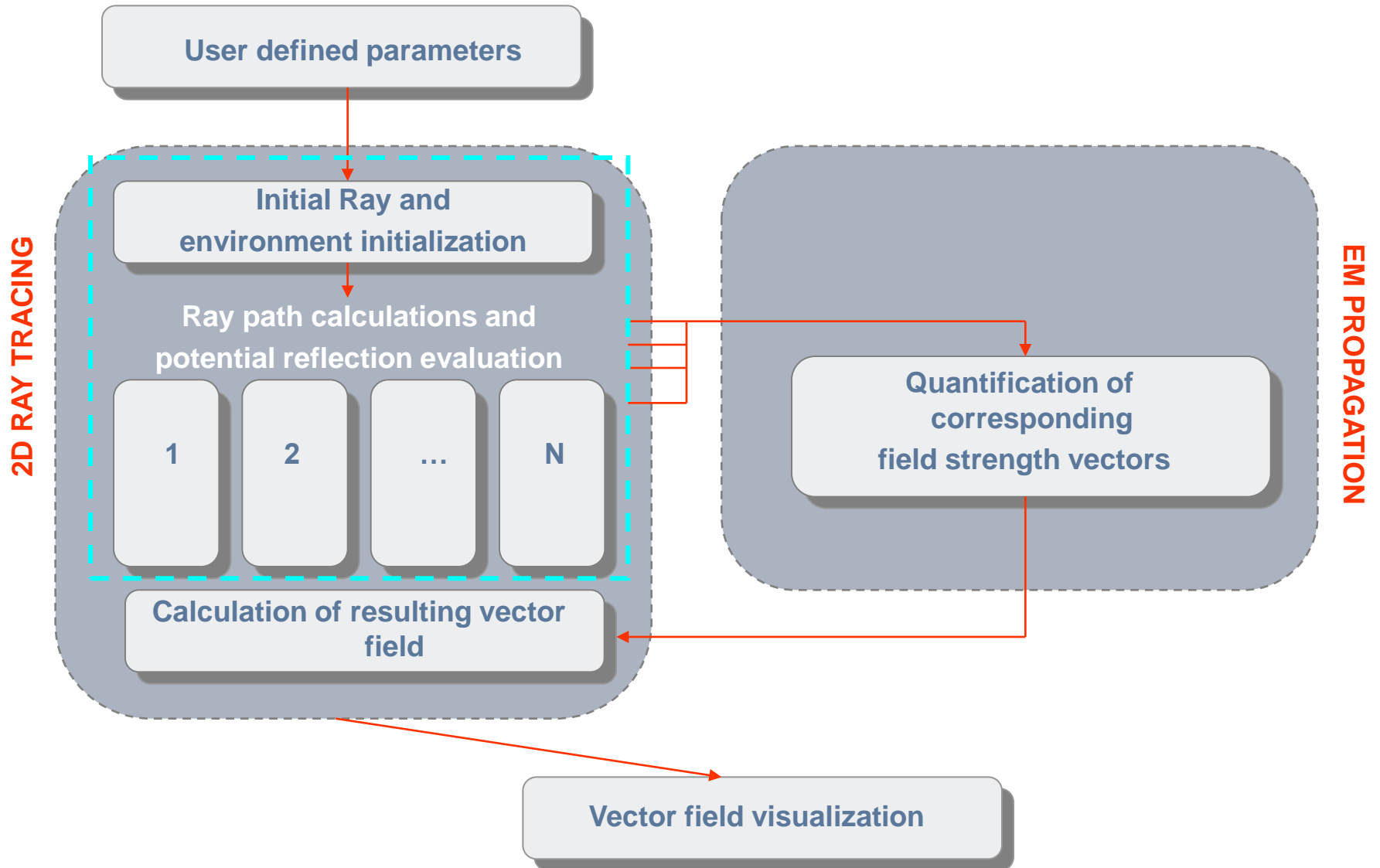
(ref: ing. Cedric Busschots)



Acceleration techniques



Acceleration techniques

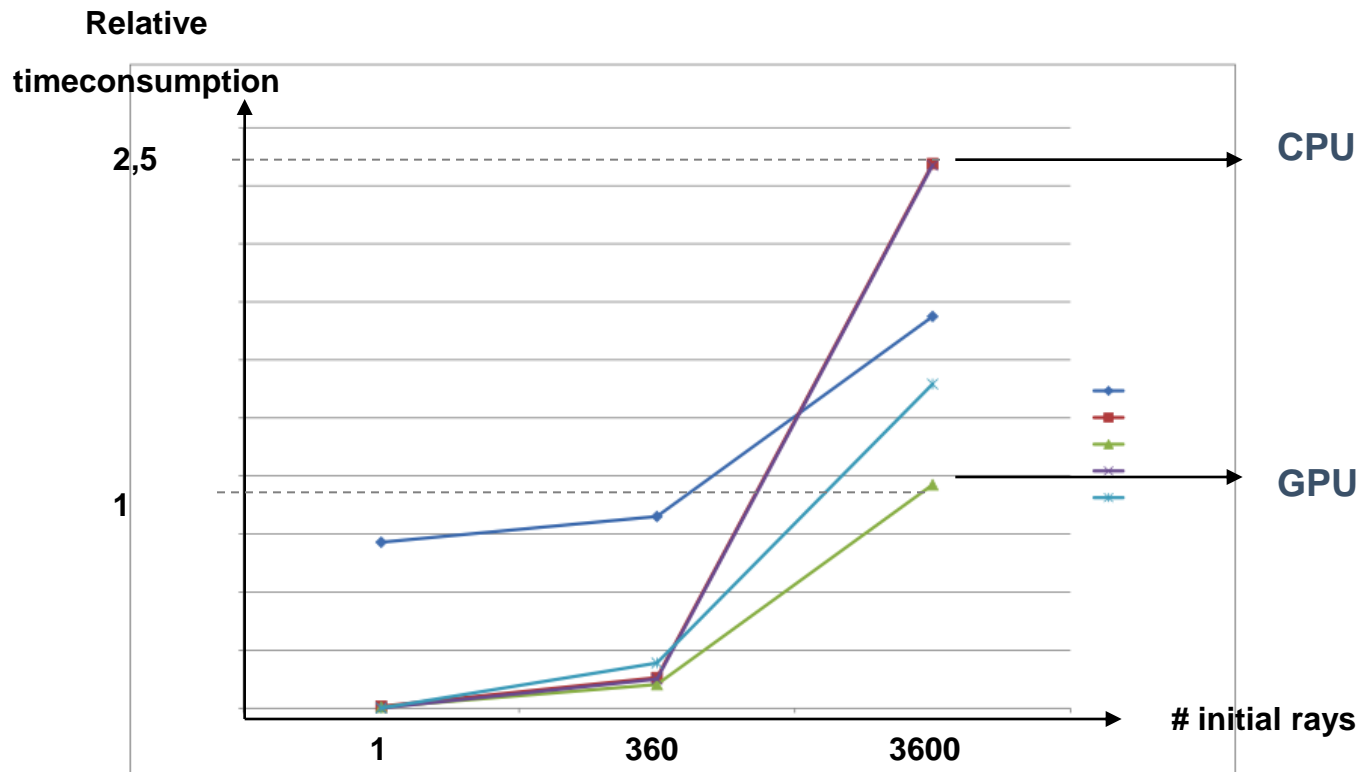


- 2D Implementation – performance analysis

(ref: ing. Cedric Busschots)

- Run time comparison for CPU and OpenCL algorithm
- Timing exercise

- Increasing #initial rays (1000 reflections)

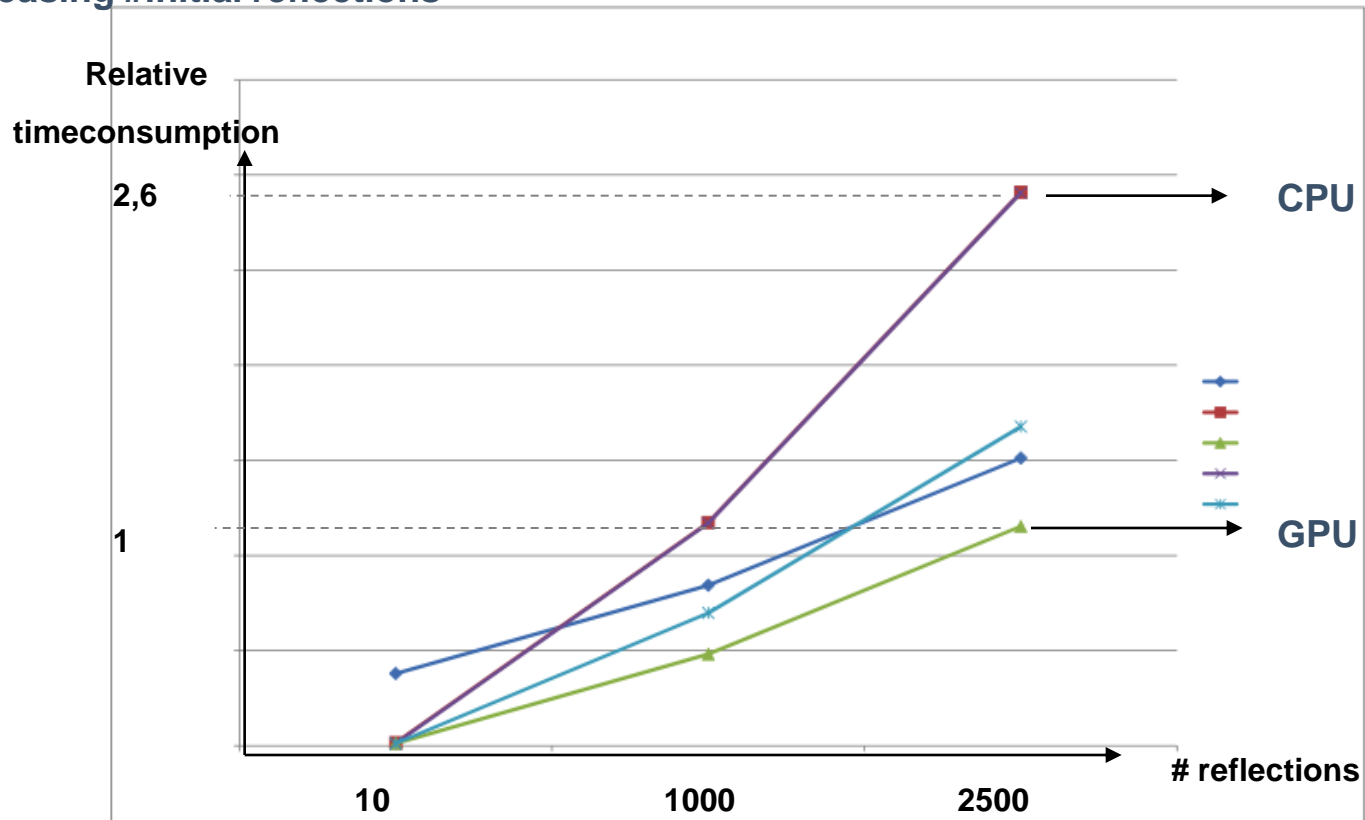


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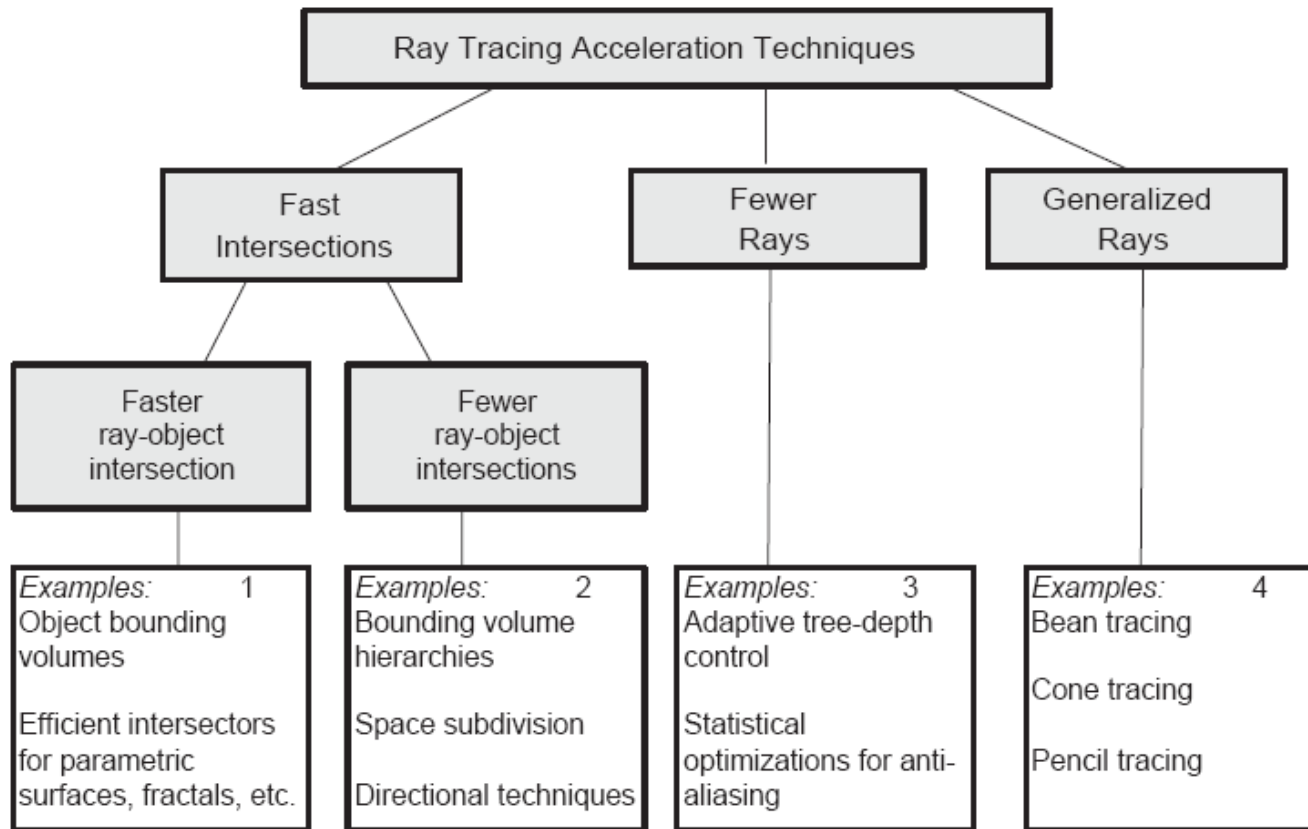


- **First conclusions**
 - **Speedup factor aprx. 2,5**
 - **Limiting boundaries are memory consumption**
 - **Further implementations needed to cover:**
 - **3D algorithm**
 - **vector calculus for polarisation and $|E|$ field magnitude**
 - **algorithm acceleration techniques**

5. Acceleration techniques

Ray tracing acceleration techniques

- Verschillende technieken beschikbaar,
echter vaak gekoppeld aan (dynamische) visualisatie toepassingen
- Generieke classificatie van acceleratietechnieken:



5. Acceleration techniques

Faster and fewer intersections

- ca. **95%** van rekentijd bij ray tracing wordt aan intersectie onderzoek besteed
- Complexiteit van standaard ray tracing intersection algoritme:

elke ray wordt met elk object vergeleken

$$|I| \times |O| \quad \begin{array}{l} I = \# \text{ initial rays (e.g. } 13 \times 10^6) \\ O = \# \text{ objects (e.g. } 10^9) \end{array}$$

=> **$O(n)$**

= complexiteit ten gevolge van sequentiële zoektocht naar individuele ray – object intersecties

= lineair zoekalgoritme

= worst case..!!

5. Acceleration techniques

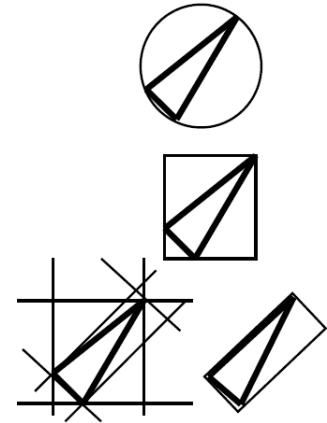
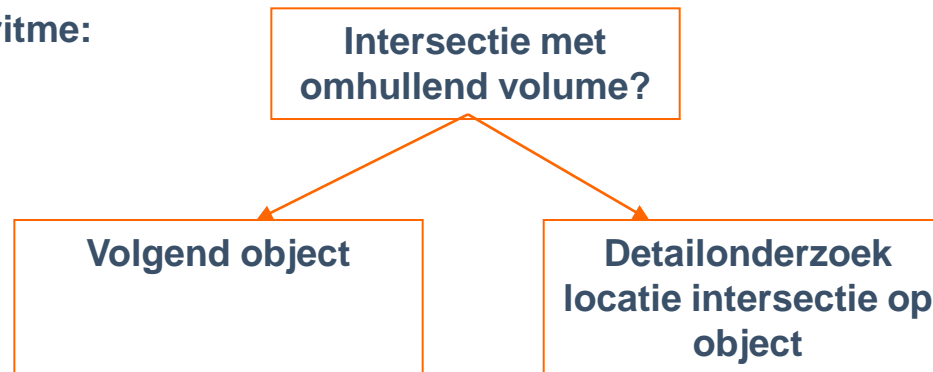
Faster and fewer intersections

- Snellere intersectie-algoritmes:

- **Object bounding volumes** hanteren:

Objecten worden omhuld door eenvoudige geometrische volumes
vb: kubus, bol, slabs (begrenzende vlakken), ...

algoritme:



Snellere berekening, afhankelijk van selectie omhullend volume

vb: Bol volume:
$$d = (\mathbf{l} \cdot \mathbf{c}) \pm \sqrt{(\mathbf{l} \cdot \mathbf{c})^2 - \mathbf{c}^2 + r^2}$$

\mathbf{l} : ray unit vector, \mathbf{c} : center, r : radius

Omhullend volume dient zo nauw mogelijk aan te sluiten aan objectgrenzen

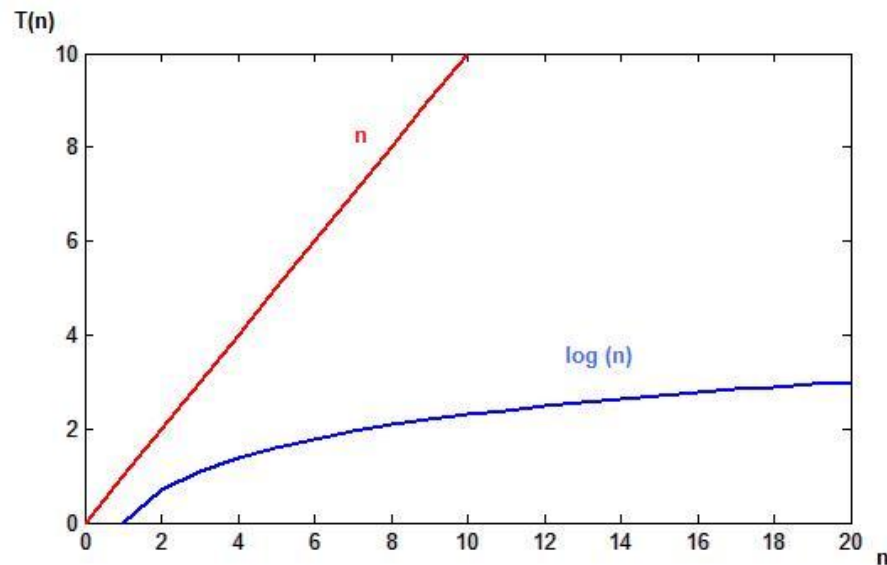
5. Acceleration techniques

Faster and fewer intersections

- Reductie aantal te onderzoeken intersecties:
- Object bounding volumes **hiërarchie** hanteren:

kleine bounding volumes worden hiërarchisch georganiseerd in nieuwe bounding volumes

Tijdens zoekalgoritme wordt de hiërarchische structuur gevolgd
=> complexiteit $O(\log n)$



5. Acceleration techniques

Faster and fewer intersections

- Reductie aantal te onderzoeken intersecties:
- Object bounding volumes **hiërarchie** hanteren:

Vorbereitung nodig: recursief opbouw algoritme

- 1) initialisatie bij algemeen omhullend volume
- 2) Opdeling voorgaand volume in deelvolumes

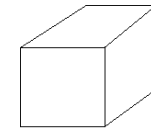
- Octree

- BSP (Binary Space Partition):

voorgaande scene-partitie halveren -> binary search tree

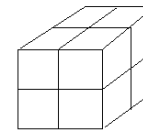
- kD-tree (k-dimensionale boom) = axis aligned BSP

objectverdeling in functie van vereiste detaillering object

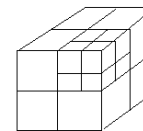
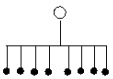


(root)

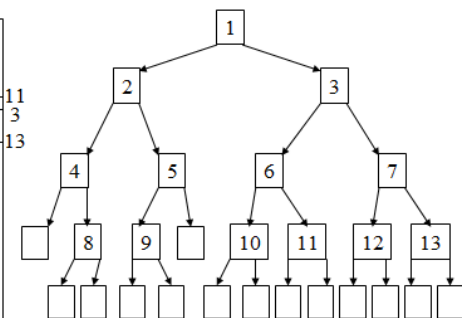
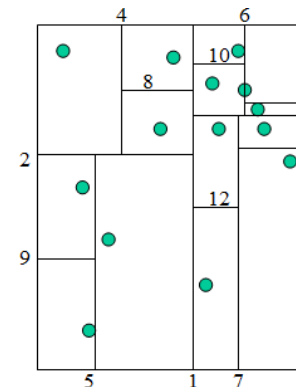
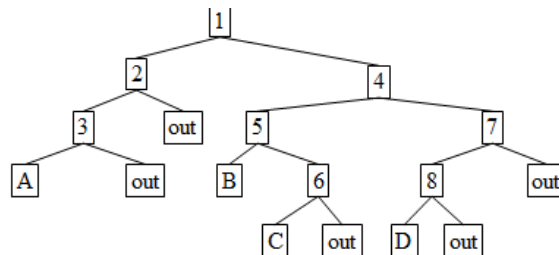
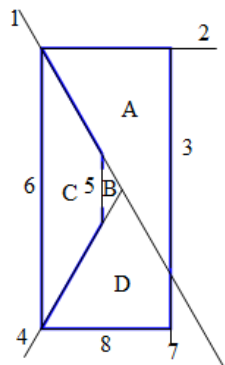
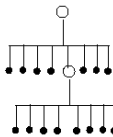
•



(1 level)



(2 levels)



Vorbereitung vraagt eveneens typisch $O(\log n)$... -> afweging

5. Acceleration techniques

Faster and fewer intersections

- Bounding volume hierarchie
- **Spatial partitioning in voxels**

- Default methode (ref: Andrew Woo, John Amanatides)

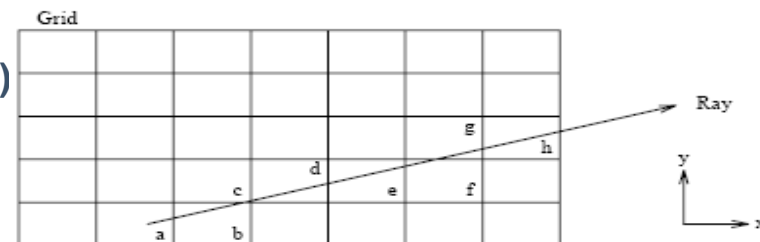
- Opdeling van ruimte in niet overlappende gebieden (voxels)
 - Octrees, eventueel met variërende grootte (ref: Glassner)
 - 3D Grid partitioning (identieke grootte per voxel)
- elke voxel bevat lijst met objecten die binnen deze voxel vallen
- per voxel enkel intersecties onderzoeken van ray met objecten die behorende tot de lijst van die voxel

- intersectie vastgesteld
- geen intersecties

=> berekening nieuwe reflected ray path

=> traversal algoritme toepassen

- Toepassing ray traversal algoritme: zoek naburige voxel
vb: 3D DDA
(3 dimensional digital difference analysis)



5. Acceleration techniques

Faster and fewer intersections

Principe:

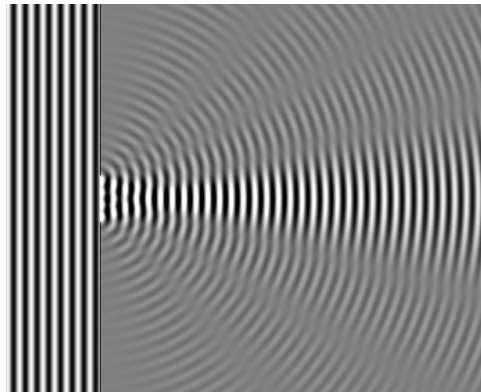
- Toepassing bounding volume hiërarchie op vaste elementen buiten virtual volume (mode stirrer, bijgevoegde absorbers, detailelementen Reverb Room, ...)
- Toepassen spatial partitioning in voxels voor virtual volume
per voxel eveneens data veldsterkte en polarisatie bewaren
laat toe bepaling 3D E-veld

Voordeel: reductie complexiteit tav eerste implementatie

Nadeel: nog geen reductie omvang data in cache (cache overflow!)

Opm: - structuur algoritmes: recursief, SIMD

- Diffractie..?



5. Acceleration techniques

Fewer rays

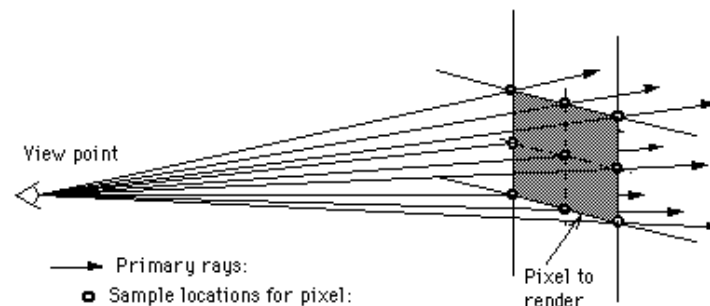
Werd reeds toegepast:

- afbreken van ray bij intersectie van dempend materiaal ($\Gamma = 0$)
- afbreken van ray bij demping in functie van afgelegde weg ($|E| \sim 1/r$)
- Begrenzing op aantal intersecties

Generalized rays

Beam, cone of pencil tracing

- Bepalen of naburige rays, of rays binnen het frustrum een identiek pad afleggen
- voordeel: simulatie wave fronts
- Nadeel : beperkte verbetering complexiteit bij EM simulatie, eerder gehanteerd bij illumination tgv diffuse reflecties



Optimal programming techniques

- Algoritmiëk:
 - Dynamic programming ?
 - Divide & Conquer ?
 - ...
- Gebruik optimale datastructuren ?
- ...